



## Review of cyclic soil behavior and input parameters for seismic site response analyses and liquefaction

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### Abstract

During earthquakes soil deposits are exposed to all kinds of seismic waves and are consequently subjected to three-directional cyclic loading and straining. In the geotechnical earthquake engineering practice, however, the analyses of such complex response of the deposits to seismic forces, the site response analyses, are typically reduced to the analyses of the effects of the vertically propagating plane shear waves through horizontally layered deposits. The popular geotechnical laboratory tests for simulation of such behavior are cyclic simple shear, cyclic triaxial, cyclic torsional and resonant column tests that all cyclically shear the soil specimen in just one direction, typically in series of cycles with constant amplitude of shear stress,  $\tau_c$ , or shear strain,  $\gamma_c$ . The paper presents several fundamental aspects of the cyclic soil behavior obtained relatively recently in the cyclic simple shear tests, indicating that the basic research of cyclic and dynamic soil properties is still going on. The parameters and curves derived from cyclic simple shear tests that are used in popular computer models for site response analyses that are treated in this paper include: maximum shear modulus,  $G_{max}$ , cyclic secant shear modulus,  $G_s$ , equivalent viscous damping ratio,  $\lambda$ , curve of the reduction of the first cycle  $G_s$  with  $\gamma_c$ , second cycle  $\lambda$  versus  $\gamma_c$  curve, pore water pressure change with the number of cycles  $N$  in saturated soils, change of  $G_s$  with  $N$ , and the cyclic threshold shear strains for pore water pressure change,  $\gamma_{wp}$ , and cyclic degradation,  $\gamma_{td}$ .

**Key words:** soil, earthquakes, cyclic loading, shear modulus, damping, strain rate, frequency, threshold strain, cyclic degradation, cyclic pore water pressure, simple shear testing

# 1 Input parameters for seismic site response analyses

The response of civil engineering structures to seismic shaking depends on the complex 3-dimensional cyclic stress-strain properties and behavior of soils in subsurface layers due to 3-directional loading. In practice, however, it is typical to consider just vertical propagation of plane shear waves through horizontally layered soil deposit such that the soil's stress-strain conditions are those of pure shear stresses,  $\tau$ , and associated shear strains,  $\gamma$ , applied cyclically in just one direction on top of the existing vertical and horizontal effective stresses  $\sigma'_{vc}$  and  $\sigma'_{hc}$ . Under such conditions the stress-strain behavior is described by cyclic loops that can be obtained from one-directional cyclic loading tests, such as cyclic simple shear, cyclic triaxial, cyclic torsional and resonant column. In these tests soil is typically subjected to series of cycles with constant amplitude of shear stress,  $\tau_c$ , or shear strain,  $\gamma_c$ . The test that most directly simulates the cyclic pure shear stress conditions is the cyclic simple shear test [1]. In this paper the results obtained relatively recently in the cyclic simple shear devices in the soil dynamics laboratory at the University of California, Los Angeles, are presented and discussed. One of the testing devices used is presented in Figure 1.

The seismic site response analyses are performed with various computer models, such as SHAKE [4], DESRA-2 [5] and its modifications [6, 7], and DEEPSOIL [30]. In these computer codes, the soil material input parameters for each layer include the parameters and curves listed in the Abstract and treated below, so the knowledge gained from the test results presented is of practical significance because it can be employed to improve the performance of these codes.

The idealized 1<sup>st</sup> and a quarter cycles loop is presented in Figure 2. In Figure 3 are presented the second cycle loop and the two loops from a single test, the loop in the first cycle and cycle N. The parameters and curves describing the cyclic behavior presented by these loops are the variation of the 1st cycle loops with amplitude,  $\gamma_c$ , typically presented by the curves  $G_s - \log \gamma_c$ ,  $G_s/G_{s_{max}} - \log \gamma_c$ , and  $\lambda - \log \gamma_c$ . Furthermore, the change of soil stiffness under the cyclic strain-controlled shearing with constant  $\gamma_c$  in each cycle N can be described with the stiffness index,  $\delta_N$ , that measures the relative change of  $G_s$  in cycle N,  $G_{sN}$ , with respect to the initial modulus  $G_{s1}$  in the first cycle  $N=1$ :  $\delta_N = G_{sN}/G_{s1} = \tau_{cN}/\tau_{c1}$ .

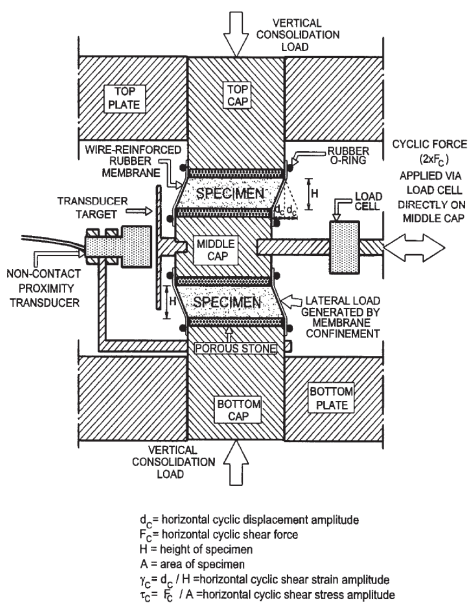


Figure 1. Setup of specimens in the UCLA dual-specimen DSS device (DSDSS device) for small-strain testing [2, 3]

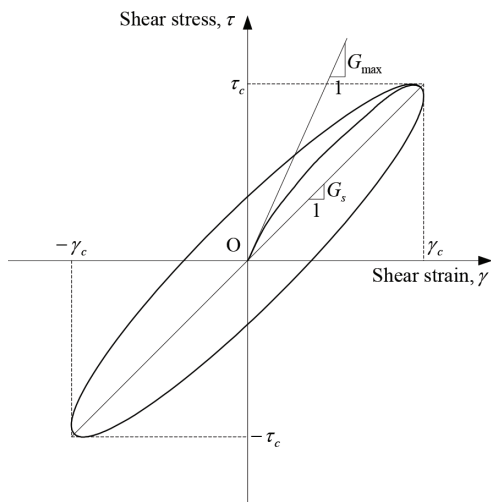


Figure 2. Idealized fully closed initial cyclic stress-strain loop (first 1.25 cycles) with definition of  $G_s$  and  $G_{max}$

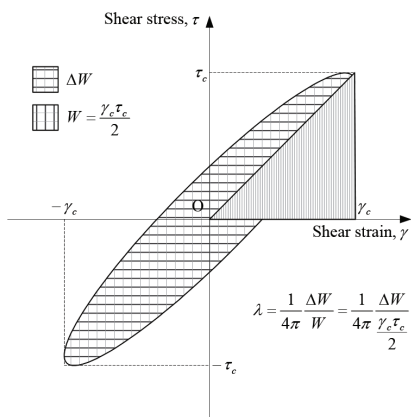
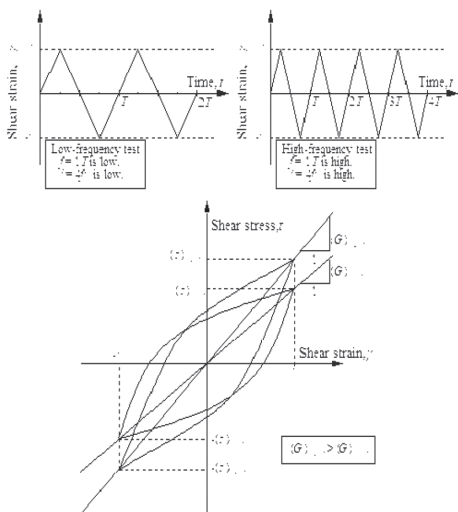


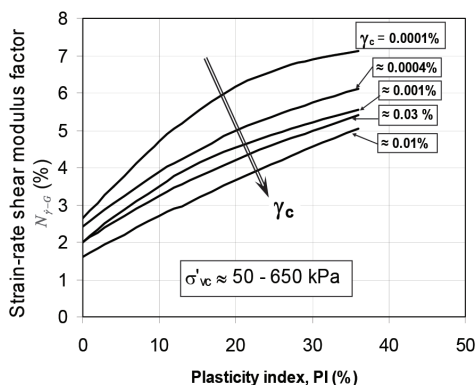
Figure 3. Definition of the equivalent viscous damping ratio,  $\lambda$  and sketch of the idealized cyclic strain-controlled behavior in the first cycle,  $N=1$ , and a subsequent cycle  $N$

## 2 Effects of the rate of shear straining and frequency on $G_s$ , $G_s/G_{\max}$ - $\log \gamma_c$ curve, $\lambda$ , and $\lambda$ - $\log \gamma_c$ curve

The parameters  $G_s$  and  $\lambda$  and the  $G_s$ - $\log \gamma_c$ ,  $G_s/G_{\max}$ - $\log \gamma_c$ , and  $\lambda$ - $\log \gamma_c$  curves are affected by many factors. One of them is the rate of shear straining  $\dot{\gamma} = d\gamma/dt$ . The effects of  $\dot{\gamma}$  encompass those of the frequency of cyclic loading,  $f$ , level of the average strain rate in a single uniform cycle,  $\dot{\gamma} = 4\gamma_c/T = 4f\gamma_c$ , where  $T$  is the cycle period, and the variation of the rate in a single cycle. How at a given  $\gamma_c$  the slope of the cyclic loop  $G_s$  changes with  $\dot{\gamma}$  is sketched in Figure 4. At a given  $\gamma_c$ , modulus  $G_s$  increases approximately linearly with the logarithm of average  $\dot{\gamma}$  and associated  $f$ . This increase can be quantified with the strain-rate shear modulus factor  $N_{\dot{\gamma}-G}$  [8] which describes the relative increase of  $(G_s)_{\text{low}f}$  due to the tenfold increases of  $\dot{\gamma}$ . Figure 5 provides the rate-of-straining effect on  $G_s$  obtained for many different soils. Two trends can be observed: (1) for any level of  $\gamma_c$  factor  $N_{\dot{\gamma}-G}$  increases consistently with  $PI$ , and (2) the rate-of-straining effect increases as  $\gamma_c$  gets smaller.



**Figure 4.** Effect of the frequency and associated average strain rate on cyclic loading behavior



**Figure 5.** General trends of the strain-rate shear modulus factor with  $PI$  and  $\gamma_c$  (from [9, 10, 11, 12])

From Figure . 5 it is also evident that the shapes of the  $G_s/G_{\max}$ - $\log \gamma_c$  curves must depend on the frequency,  $f$ , and associated average strain rate,  $\dot{\gamma}$ . In this context two types of  $G_s/G_{\max}$ - $\log \gamma_c$  curves can be constructed: curves obtained from tests with the same  $f$  at all  $\gamma_c$  levels, and curves from tests with constant  $\dot{\gamma}$  at all  $\gamma_c$  levels. Depending on whether  $\dot{\gamma}$  or  $f$  is constant, different curvatures of modulus reduction curves are obtained. If  $\dot{\gamma}$  is constant,  $G_s$  consistently decreases with  $\gamma_c$ . If  $f$  is constant,  $G_s$  decreases with  $\gamma$  at higher  $\gamma_c$ , but at low  $\gamma_c$  it may for clays increase and then decrease, which means that at

low  $\gamma_c$  the  $G_s/G_{s_{\max}} - \log \gamma_c$  curve for clay may run above  $G_s/G_{s_{\max}} = 1.0$  line. These trends are reported in [8, 9, 13]. How constant  $f$  and  $\dot{\gamma}$  curves compare for different soils is indicated in Figure . 6. The  $G_s/G_{s_{\max}} - \log \gamma_c$  curves derived from the results of DSDSS tests (Figure . 1) on a natural sandy soil (labeled Arlita-1) and a natural clay having PI=26 (labeled ESC-1) are compared. For sandy soil, the curves for two constant frequencies,  $f = 0.3$  Hz and 3 Hz, and the curves for constant values of  $\dot{\gamma}$  ranging between 0.0001 %/sec and 0.003 %/sec, plot practically on top of each other. This is because sandy soils do not exhibit noticeable effects of the rate of straining. In the case of clay, the values of  $G_s/G_{s_{\max}}$  obtained in the test series conducted at constant  $\dot{\gamma}$  (ranging again between 0.0001 %/sec and 0.003 %/sec) consistently decrease with  $\gamma_c$ , just like for sands. The values of  $G_s/G_{s_{\max}}$  obtained for clay in the test series conducted at constant frequencies of 3 and 0.3 Hz first increase with  $\gamma_c$  and then decrease. Such cyclic behavior occurs because if  $f = \dot{\gamma} / (4\gamma_c)$  is constant,  $\dot{\gamma}$  increases with  $\gamma_c$ , causing soil to respond as stiffer. These trends are also discussed in [8, 13, 9].

The effects of frequency,  $f$ , on  $\lambda$  were studied with the help of DSDSS device [14, 10]. The test results revealed that for many soils  $\lambda$  is in general the smallest at around  $f \approx 0.1$  Hz. At larger  $f$ ,  $\lambda$  is usually increasing with  $f$ , and below it usually decreases with  $f$ . Such a trend is consistent with some data presented earlier [15].

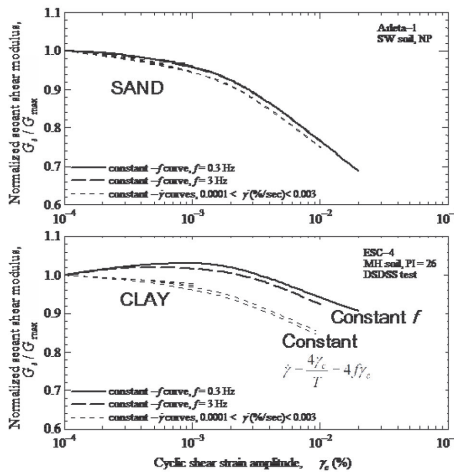


Figure 6. Example of the constant-strain-rate and constant-frequency normalized modulus reduction curves for sandy soil and clayey soil [10]

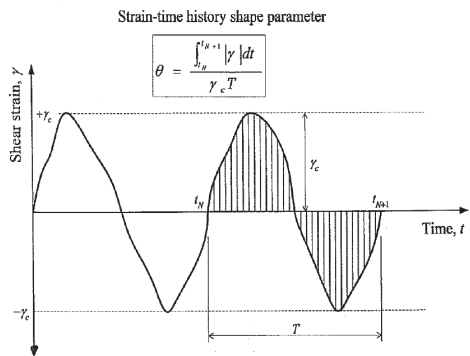
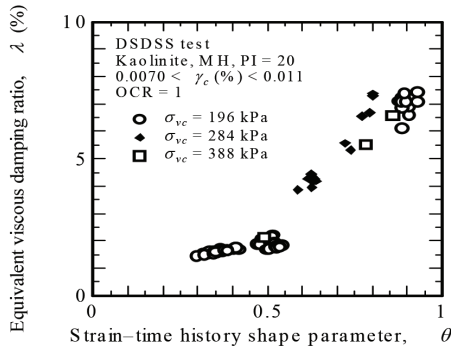


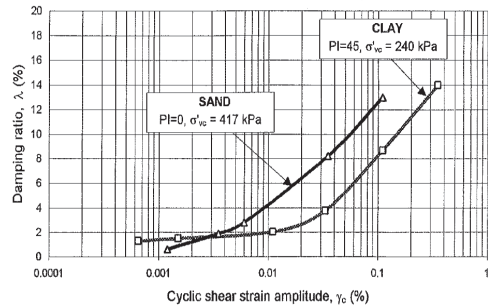
Figure 7. Definition of the strain-time history shape parameter,  $\theta$ , measuring the effect of the shape of cyclic straining on the equivalent viscous damping ratio,  $\lambda$  [16]

The variation of the rate of straining in a single cycle affects damping  $\lambda$  and is associated with the fact that a longer application of larger strains in a single cycle allows for more relaxation and creep, which is generating larger area of the loop and thus larger damping  $\lambda$ . This means that for a given  $\gamma_c$  the area of the loop can be correlated to the

absolute area under the strain-time curve. On the basis of that, a parameter called the *strain-time history shape parameter*,  $\theta$ , was defined [16], as shown in Figure . 7. For triangular cyclic straining  $\theta = 0.50$ , for sinusoidal  $\theta = 0.64$ , and for trapezoidal  $\theta \approx 0.75$ . The correlation between  $\theta$  and  $\lambda$  for kaolinite clay tested at small  $\lambda_c$  is presented in Figure . 8. It is evident that changing the shape of cyclic straining can change  $\lambda$  dramatically.



**Figure 8.** Trend of damping ratio,  $\lambda$  with the strain-time history shape parameter  $\theta$  in the range of  $\gamma_c$  from 0.007 % to 0.011 % [10]



**Figure 9.** Damping curves  $\lambda$ - $\log \gamma_c$  for sand and clay obtained for sinusoidal cyclic straining crossing each other between  $\gamma_c = 0.001$  % and 0.01 % [14]

The above effects of the shape of cyclic straining are pronounced in soils that are more susceptible to creep and relaxation. They are small to negligible in clean sands and gravels and relatively large in clayey soils and generally increase with PI. This means further that the tips of the loops of clean sands are usually pointed, regardless of the shape of cyclic straining, while the tips of the loops of clay due to sinusoidal straining are rounded [17, 18, 19]. This has interesting consequences for the shape and relative position of the  $\lambda$ - $\log \gamma_c$  damping curves for clays with respect to those for sands [20]. Due to the roundness of the tips of the loops at small  $\gamma_c$  and difference in nonlinearity between sands and clays at large  $\gamma_c$  [21], the damping curves of sand and clay cross each other in the zone between  $\gamma_c \approx 0.001$  % and 0.01 % [20], such as shown in Figure . 9. See also [22].

### 3 Threshold strains for cyclic degradation and pore water pressure in Clays

Threshold strains for cyclic degradation,  $\gamma_{td}$ , and cyclic pore water pressure,  $\gamma_{tp}$ , are fundamental cyclic soil properties [23]. If in clayey soil  $\gamma_c < \gamma_{td}$  the soil does not degrade,  $\delta_N = G_{SN}/G_{S1} = \tau_{cN}/\tau_{c1}$  practically does not change. If  $\gamma_c > \gamma_{td}$  index  $\delta_N$  decreases with N such as shown in Figure 11 for the loops presented in Figure 10. Figure 12 shows how the corresponding degradation parameters, representing the slopes of the lines in Figure 11,  $t = \log \delta_N / \log N$ , changes with  $\gamma_c$ . From this Figure  $\gamma_{td} = 0.012$  % can be derived.

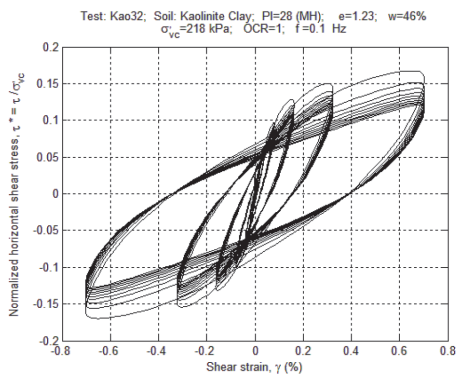


Figure 10. Stress-strain loops from cyclic strain-controlled simple shear tests on kaolinite clay [24, 25]

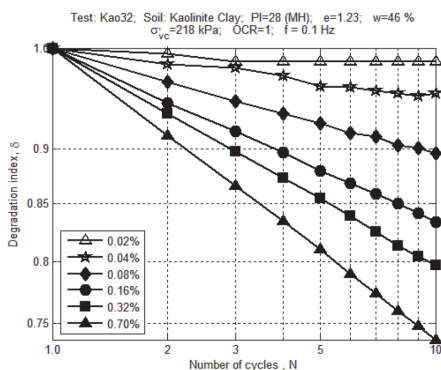


Figure 11. Cyclic degradation in the cyclic strain-controlled tests on kaolinite clay [24, 25]

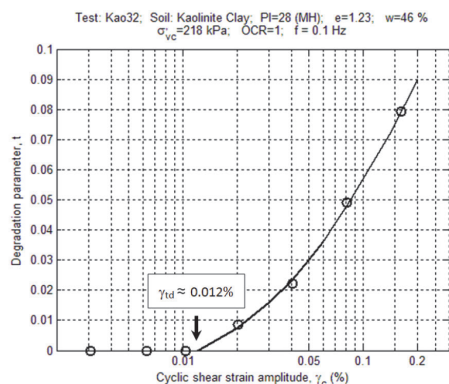


Figure 12. Variation of the degradation parameter, \$t\$, with the cyclic shear strain amplitude, \$\gamma\_c\$ [24, 25]

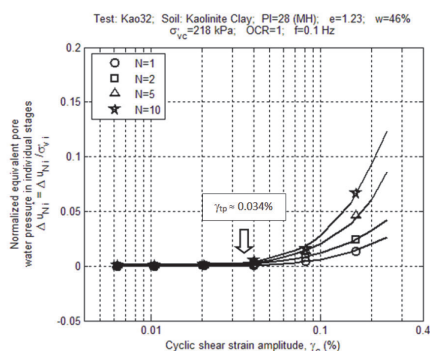


Figure 13. Change of the cyclic pore water pressure \$\Delta u\_N^\*\$ with \$\gamma\_c\$ in the cyclic strain-controlled tests on normally consolidate kaolinite clay [24, 25]

Figure 13 shows the change of normalized cyclic pore water pressure  $\Delta u_N^* = \Delta u_N / \sigma'_{vc}$  with  $\gamma_c$  for the tests results presented in Figure 10, where  $\Delta u_N$  is the pore water pressure at the end of cycle  $N$ . From this Figure  $\gamma_{tp} = 0.034\%$ . Accordingly, from the same test results  $\gamma_{tp}$  is greater than  $\gamma_{td}$ . Such difference between  $\gamma_{td}$  and  $\gamma_{tp}$  obtained for many soils is displayed in Figures 14 and 15.

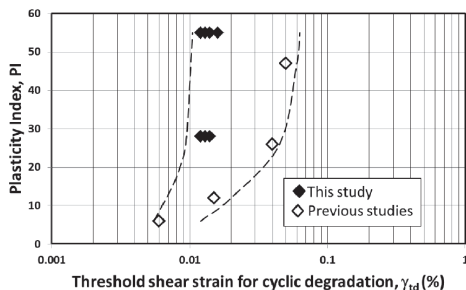


Figure 14. Relationship between the threshold shear strain for cyclic degradation,  $\gamma_{td}$ , and soil's plasticity index, PI [composed from 10, 24, 25, 26]

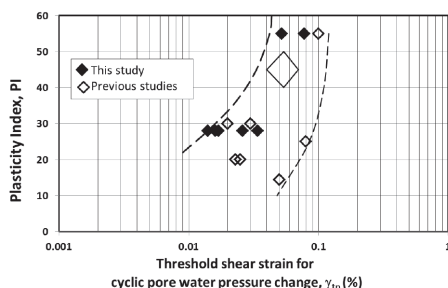


Figure 15. Relationship between the threshold shear strain for cyclic pore water pressure change,  $\gamma_{tp}$ , and soil's plasticity index, PI [24, 25]

## 4 Cyclic secant shear modulus and pore water pressure change in sands at small cyclic strains

Figure 16 shows the recent results of tests equivalent to those presented in Figure 10, but conducted on saturated sand instead of clay. They reveal that at the cyclic shear strain amplitudes,  $\gamma_c$ , between 0.01 % and 0.10 to 0.15 % the secant shear modulus at cycle N,  $G_{sN}$ , first increases with N, for up to 10 % of the initial  $G_{s1}$ , and then decreases, while the cyclic pore water pressure,  $\Delta u_N$ , monotonically increases, and that  $\Delta u_N$  can actually reach up to 40 % of the initial effective vertical stress before  $G_{sN}$  drops below  $G_{s1}$  and sands start to truly degrade [24, 27, 28, 29]. They also demonstrate that the effective stress principle, to the extent that it stipulates that if the pore water pressure increases during cyclic loading and the effective stress decreases, the sand stiffness and strength must decrease, is not universally valid. This should have significant impact on the analyses of the liquefaction seismic site response.

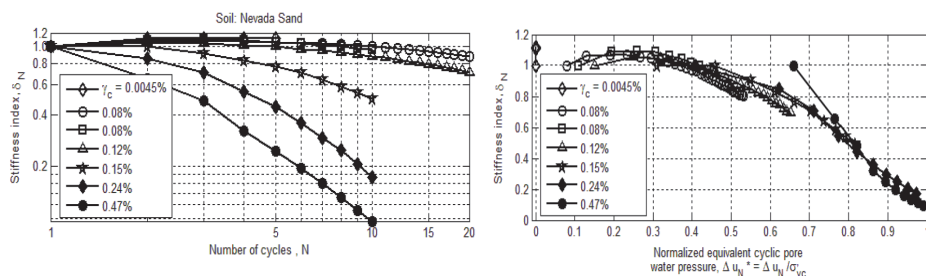


Figure 16. Variation of stiffness index,  $\delta_N$ , with the number of cycles, N, and its relationship with cyclic pore water pressure,  $\Delta u_N^*$ , obtained in the simple shear cyclic strain-controlled tests on Nevada sand [24, 27]



## 5 Conclusions

The results presented in this paper and corresponding references obtained relatively recently, in particular the results in section 4 above, show that there are still fundamental aspects of the cyclic behavior of soils that need to be tested and clarified. They also indicate that seismic site response models can be more accurate if recent discoveries are incorporated in their inputs. After decades of experimental research, the high quality laboratory cyclic testing of soils, especially at small cyclic strains, is still a basic tool for the advancement of our understanding of the effects of earthquakes on civil engineering structures.

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