

LOCAL EARTHQUAKES - GROUND MOTION MODELS FOR EPICENTRAL ZONE

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Abstract

Based on records on occurred shallow earthquakes obtained on soil type rock, epicentral distances of $R_e \leq 20\text{ km}$, focal depths $h \leq 10\text{ km}$ and local magnitude $M = 3.9 - 6.1$, ground motion models GMMs for an epicentral zone were developed. Investigated were horizontal acceleration response spectrum SA for 5% of the critical damping and for 221 models of a single-degree-of-freedom system with a natural period ranging from 0.01 to 5.0 seconds.

Two mathematical physical models were selected. In the first one, the horizontal acceleration response spectrum SA was dependent on magnitude only, whereas in the second one, it depended on both magnitude and hypocentral distance. For an assumed normal distribution of the natural logarithm of SA , a multi-linear regression analysis was carried out. The results were regression coefficients and standard deviations. These are practically applicable for prediction of the expected SA in an epicentral zone by deterministic and probabilistic methods.

Keywords: ground motion models, spectral acceleration, epicentral zone, magnitude, epicentral distance

1. Ground motion models – GMMs

GMMs predict the expected level of ground motion depending on magnitude, distance, type of fault structure, local soil layers, azimuth, etc. They are empirical since they are developed by use of data from records of occurred earthquakes and using the regression analysis method. The selected mathematical form will fit in an available or formed databank of records of occurred earthquakes for an assumed normal or log-normal distribution of parameters on which earthquake ground motion depends. The result are regression coefficients and standard deviations. Such GMMs are called conventional /or traditional [1, 7, 8, 12]. Today, GMMs are also developed by use of machine learning approaches ML [6], which cannot be a replacement for the conventional ones. Therefore, the presented conventional GMMs in this paper are important for prediction of the seismic effect in an epicentral zone.

According to summary reviews of a large number of published GMMs [2, 3], it is evident that the number of GMMs for local earthquakes is very small [1, 6, 7, 12].

2. GMMs for Local Earthquakes as a Necessity

As a long year researcher [8, 10, 12] and user of GMMs [9, 11, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23], the author has understood their great importance when probabilistic PSHA [9, 11, 13, 14, 19, 22, 23], and deterministic DSHA [9, 11, 13] methods are used for definition of seismic design parameters. Therefore, the development of GMMs for local earthquake effects is a necessity according to the author. This particularly holds for an epicentral zone and existence of shallow soil layers of weak characteristics that are great amplifiers of local and regional seismic effects upon seismic rock. The dynamic response of their characteristic soil model, upon the ground surface or at the foundation level, known as specific site spectrum SSS, very often surpasses the design spectra recommended and given in the valid standards.

SSS is particularly important in design of seismically resistant structures of the first class of importance, located in the immediate vicinity of active fault structures with the potential to generate local earthquakes with $M > 6.5$ according to Richter and Eurocode 8 [4, 5], moment magnitudes $M_w > 6.5$, according to UBC 2000 [24], and defined characteristic of local soils. Therefore, the regulations for design of seismically resistant structures [4, 5, 24] also contain defined principles and rules for its determination as well as criteria for its selection as a design spectrum of a site.

2.1. GMMs for Epicentral Zone

GMMs for an epicentral zone were investigated within the frames of the scientific-research project: Ground Motion Models [10]. The created databank of recorded accelerograms of occurred earthquakes obtained by SMA- instruments, Kinematics, from the strong motion instrument network of former Yugoslavia [8] and the Italian databank ENEA-ENEL (ENEA-ENEL: File ENEAUN TUTTO C VM/HPO 4.2 CMSL–SIAM– 8.4.87) were used. The recorded accelerograms contained in both banks were available as corrected time histories of acceleration.

These were used to create two separate datasets with different distribution of time histories of acceleration per earthquake parameters like magnitude M , epicentral distance R_e , focal depth h and local soil conditions. All this for the purpose of investigating the effect of the distribution of data upon the size of the expected SA in an epicentral zone.

Two sets of data were investigated:

I set 59 data: $h \leq 10 \text{ km.}, R_e \leq 20 \text{ km.} (M = 3.9 - 6.1, R_h = 7 - 30 \text{ km.}, h = 5 - 10 \text{ km.})$

II set 101 data $h \leq 20 \text{ km.}, R_e \leq 35 \text{ km.} (M = 3.9 - 6.5, R_h = 7 - 40 \text{ km.}, h = 5 - 17 \text{ km.})$

Computed were the horizontal acceleration response spectra for 5% of the critical damping $SA(T; \xi = 0.05)$ for 221 models of a single-degree-of-freedom system with periods ranging from 0.01 second to 5.0 seconds for each of the two data sets.

Two mathematical models (equations 1 and 2) were selected and fitted into each of the two created data sets.

$$\text{GMM1:} \quad \ln SA(T; \xi = 0.05) = b_1 + b_2 M + \sigma_{\ln SA} P \quad (1)$$

$$\text{GMM2:} \quad \ln SA(T; \xi = 0.05) = b_1 + b_2 M + b_3 \ln R_h + \sigma_{\ln SA} P \quad (2)$$

$$R_h = \sqrt{(R_e)^2 + h^2} \quad (3)$$

where: $SA(T; \xi = 0.05)$ is the amplitude of the horizontal acceleration response spectrum for 5% of the critical damping in (cm / s^2), M is local magnitude according to Richter, R_h is hypocentral distance in km. , R_e is epicentral distance in km. , h is focal depth in km. , b_1, b_2, b_3 are regression coefficients, $\sigma_{\ln SA}$ is standard deviation, and P is random variable, with a value of zero for median and 1 for median plus one standard deviation.

The first GMM1 (Equation 1) is a function of magnitude M , i.e., of the earthquake energy, whereas the second GMM2 is a function of magnitude M and hypocentral distance R_h (Equation 2). In both equations, the term depending on the local soil conditions is omitted since the selected time histories of acceleration are obtained for the same type of soil, i.e., rock.

The size of SA amplitudes is directly proportional to the size of magnitude M and inverseley proportional to the size of distance R_h . Therefore, in the first GMM1, SA depends on M only, whereas in the second GMM2, SA depends on both M and R_h . With the application of both models, the assessment of the seismic effect in the epicentral zone is much more realistic.

A multi linear regression analysis was carried out for an assumed normal distribution for $\ln SA$. In it, the dependent parameter was $\ln SA$. Independent parameters were M for GMM1, and M and R_h for

GMM2. For each of both GMMs, 221 regression analyses were performed. Regression coefficients and standard deviations were obtained.

It was for the first time that GMMs obtained with the first set of data (Tables 1 and 2) were published. The results obtained with the second data set (containing also the data from the first set) or a total of 101 horizontal acceleration components, were published in 2008 [12], but are not presented for all 221 models of a single-degree-of-freedom system, but only for selected 43 (Note: equations 1 and 2 of these investigations also hold for the GMMs published in 2008. In these, there is a typing error. Specifically, in the mathematical equations, regression coefficient b_1 without \ln before it, or the same as in eq. 1 and 2 herein, should be used). GMMs defined with the two sets of data refer to an epicentral zone. The difference is that some of these are for very shallow earthquakes with focal depth of down to 10 km, epicentral distances of up to 20 km and magnitudes between 3.9 and 6.1, whereas the others are for shallow local earthquakes with focal depths of down to 20 km, epicentral distances of up to 35 km and magnitudes between 3.9 and 6.5.

Using the results shown in Table 1 (GMM1, equation 1), horizontal acceleration response spectra SA for an expected earthquake with $M = 6.5$ were computed as median and median + one standard deviation (Figure 1, above). The comparison between these and those computed with GMM2 (Table 2, equation 2) for $M = 6.5$ and $R_h = 7$ km, as median and median + 1 standard deviation, is presented type A (Figure 1, above and below). Such a direct comparison between a deterministic spectrum and a probabilistic spectrum, given according to the European standard /or other valid standard, can be made for all cases when such comparison is required by regulations or recommendations. Namely, during definition of maximum possible earthquake on locations of structures of capital importance, particularly when no regulations are elaborated for them, as are large dams [13, 15]. In other cases, it is necessary to compute a probabilistic spectrum by seismic hazard analyses PSHA, for a defined return period, applying GMMs developed for an epicentral zone. If used as alternative in PSHA, they should be given a corresponding weight factor. The results from the PSHA should be compared to the design ones given in Eurocode 8, for corresponding return periods.

In completely the same way as in Figure 1 (above and below), Figure 2 (above and below) shows the horizontal acceleration response spectra SA for GMM1 and GMM2, for the same values of magnitude and hypocentral distance ($M = 6.5$, $R_h = 7$ km), as median and median + 1 standard deviation, for earthquakes with hypocentral depth of down to 20 km [12].

The effect of M and R_h for deeper local earthquakes ($h \leq 20$ km.) is given in Figure 3 (above and below). GMMs defined with the two equations and with the second data set, or 101 data [12], were used. The acceleration spectra SA for a single value of magnitude, ($M = 6.5$), and varied values of $R_h = 5, 7, 10, 20, 40$ km are shown in Figure 3 (above), while for a single value of $R_h = 10$ km and varied values of $M = 4.5$ to 6.5, by a step of 0.5, they are given in Figure 3 (below). Figure 3 (above) shows that SA , for the range of periods $T > 0.4$ seconds, are decreased with the increase of R_h , whereas for $T < 0.4$ seconds, they are increased (the red line). For the same hypocentral distance, $R_h = 10$ km, and increase of magnitude M , SA are increased for the range of $T > 0.3$ seconds, while they are negligibly reduced for the range $T < 0.3$ seconds (black line).

3. Conclusions

The presented regression coefficients and standard deviations, for two mathematical models of ground motion, for soil type - rock, are practically applicable in defining the seismic design parameters by deterministic and probabilistic methods. While using them, care should be taken for the values of the boundaries of magnitude, epicentral distance and focal depth for which they are used, for the purpose of avoiding the extrapolation effect or making a mathematical error. While using very small hypocentral depths that are smaller than the least included in the data, it is recommended to use a mathematical model in function of magnitude.

The investigations presented herein are a contribution to better inclusion of the effect of local earthquakes in providing seismic resistance of structures.

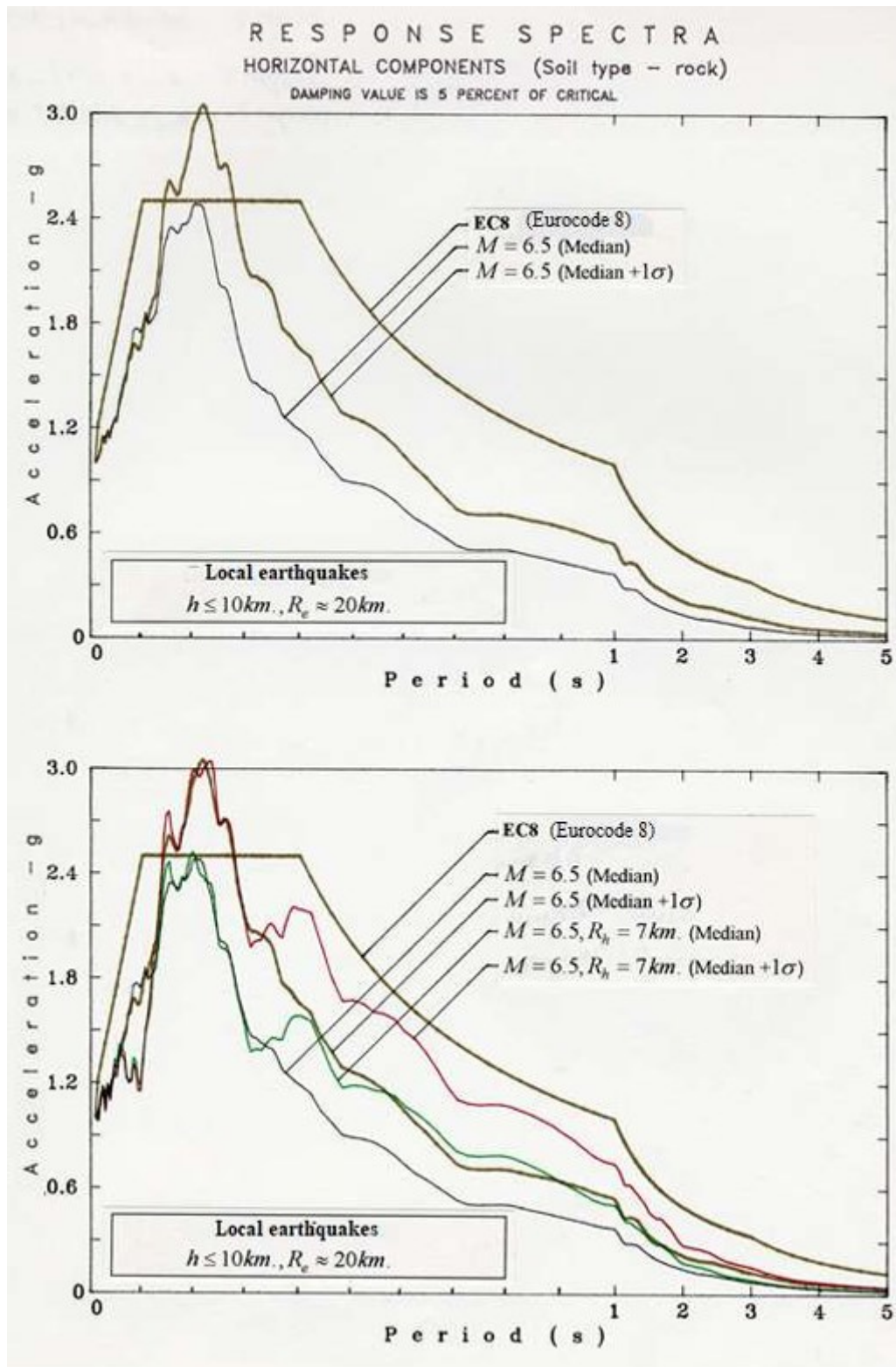


Figure 1. Comparison between expected SA (g) for an epicentral zone, for GMM1 (the figure above) and GMM2 (the figure below) and Eurocode 8.

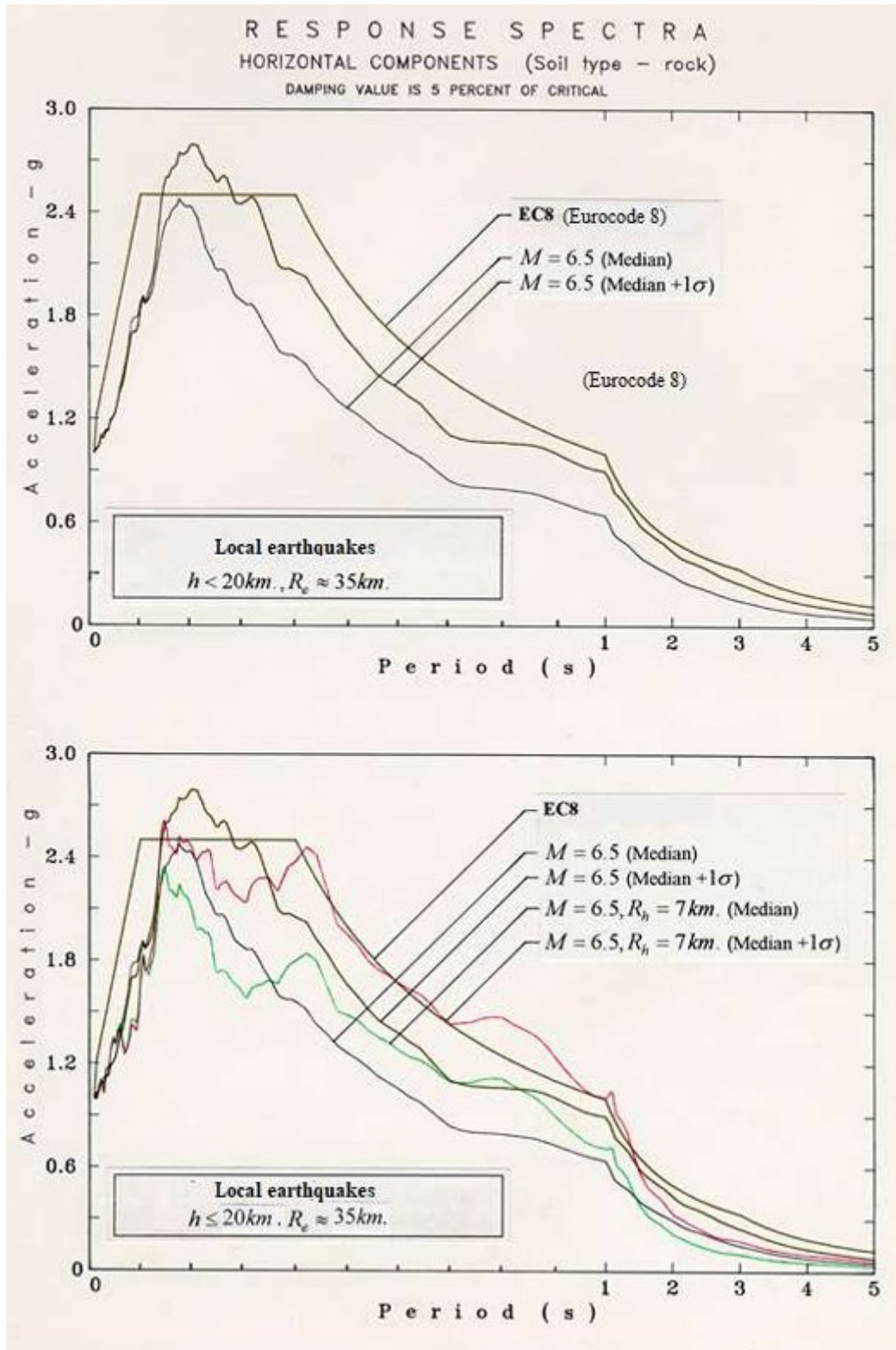


Figure 2. Expected SA (g) for an epicentral zone, for GMM1 (the figure above) and GMM2 (the figure below) and comparison with Eurocode 8.

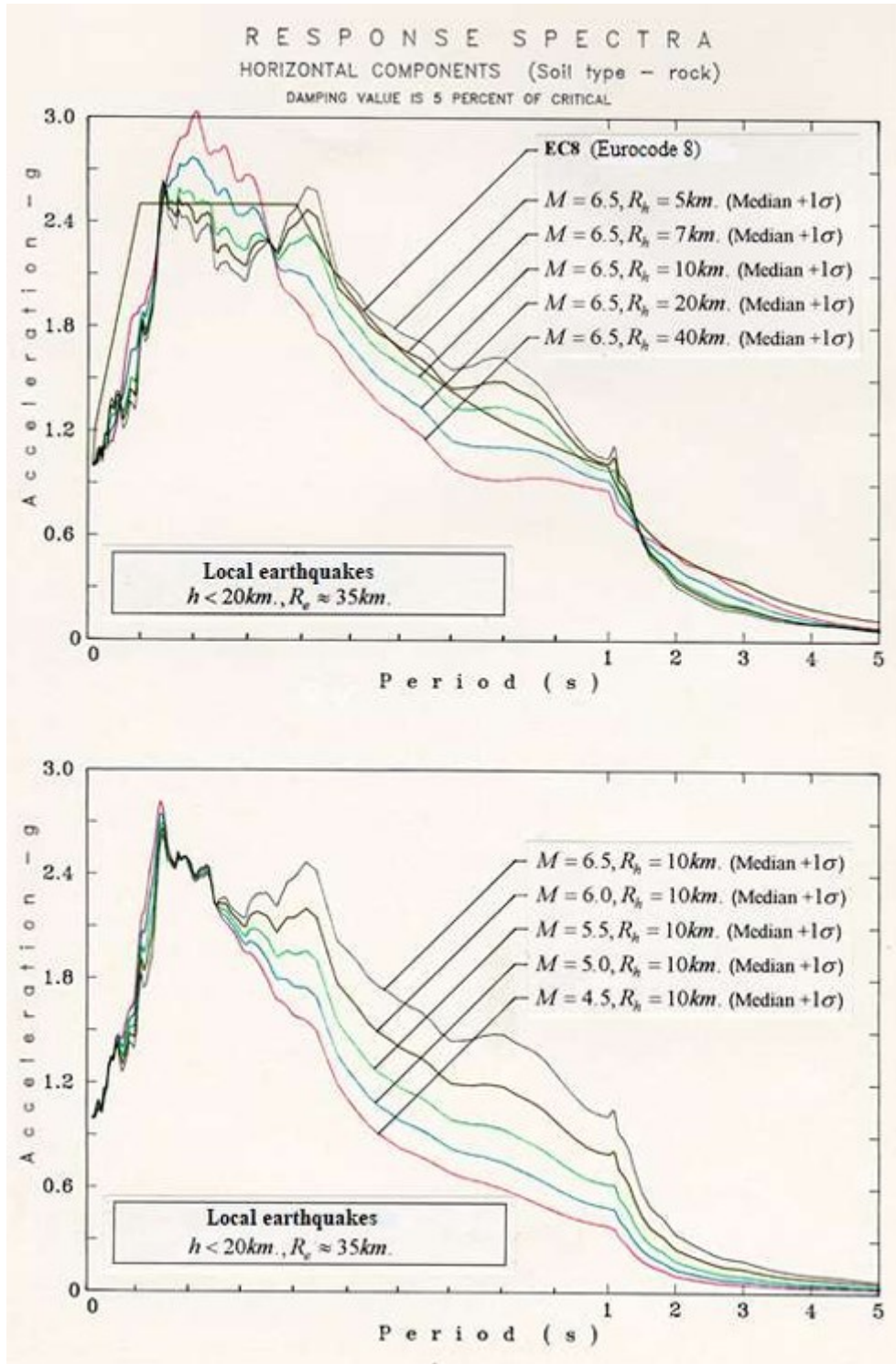


Figure 3. Distribution of expected SA (g) for an epicentral zone for GMM2 (the figure below) and comparison with Eurocode 8 (the figure above).

Table 1. Regression coefficients and standard deviation
Mathematical model: $\ln SA(T; \xi = 0.05) = b_1 + b_2 M + \sigma_{\ln SA} P$

No.	Period T (s)	b_1	b_2	$\sigma_{\ln SA}$	No.	Period T (s)	b_1	b_2	$\sigma_{\ln SA}$
1	0.0100	2.7280	.2865	.5958	59	0.290	3.1373	.2971	.9134
2	0.0145	2.7310	.2908	.5847	60	0.295	3.1592	.2885	.9179
3	0.0190	2.6465	.3092	.5920	61	0.300	3.1789	.2808	.9278
4	0.0235	2.5599	.3343	.5898	62	0.305	3.1890	.2755	.9366
5	0.0280	2.7046	.3101	.5711	63	0.310	3.1782	.2754	.9433
6	0.0325	2.6892	.3186	.5766	64	0.315	3.1531	.2792	.9452
7	0.0370	2.8587	.2894	.5792	65	0.320	3.1297	.2816	.9493
8	0.0415	2.9389	.2839	.5896	66	0.325	3.1090	.2830	.9541
9	0.0460	2.9838	.2820	.5797	67	0.330	3.0666	.2887	.9579
10	0.0505	3.0690	.2697	.5759	68	0.335	3.0258	.2935	.9611
11	0.0550	3.1238	.2725	.5791	69	0.340	2.9773	.3000	.9587
12	0.0595	3.2308	.2640	.5633	70	0.345	2.9209	.3083	.9516
13	0.0640	3.3098	.2576	.5739	71	0.350	2.8837	.3122	.9438
14	0.0685	3.4338	.2414	.5728	72	0.355	2.8660	.3118	.9360
15	0.0730	3.4811	.2436	.5830	73	0.360	2.8716	.3068	.9301
16	0.0775	3.6054	.2289	.5626	74	0.365	2.8798	.3012	.9260
17	0.0820	3.5816	.2419	.5504	75	0.370	2.8609	.3021	.9289
18	0.0865	3.6808	.2278	.5407	76	0.375	2.8288	.3056	.9299
19	0.0910	3.8249	.2052	.5257	77	0.380	2.7960	.3090	.9320
20	0.0955	4.0689	.1656	.5435	78	0.385	2.7676	.3117	.9337
21	0.100	4.1839	.1518	.5586	79	0.390	2.7515	.3123	.9314
22	0.105	4.1673	.1605	.5794	80	0.395	2.7382	.3129	.9276
23	0.110	4.2340	.1446	.6043	81	0.400	2.7329	.3125	.9267
24	0.115	4.2185	.1483	.6361	82	0.420	2.6917	.3125	.9386
25	0.120	4.2124	.1512	.6525	83	0.440	2.7506	.2894	.9425
26	0.125	4.2442	.1486	.6460	84	0.460	2.6613	.2932	.9465
27	0.130	4.1652	.1696	.6491	85	0.480	2.5702	.2958	.9498
28	0.135	4.0044	.2044	.6777	86	0.500	2.4156	.3173	.9435
29	0.140	3.7978	.2454	.6967	87	0.520	2.2638	.3388	.9367
30	0.145	3.6550	.2711	.7086	88	0.540	2.0909	.3626	.9277
31	0.150	3.5136	.2966	.7051	89	0.560	1.9356	.3808	.9314
32	0.155	3.4297	.3099	.6965	90	0.580	1.8709	.3826	.9353
33	0.160	3.3998	.3134	.6905	91	0.600	1.8471	.3752	.9441
34	0.165	3.4233	.3085	.6858	92	0.620	1.8563	.3628	.9519
35	0.170	3.4275	.3086	.6865	93	0.640	1.8525	.3554	.9459
36	0.175	3.3737	.3198	.6991	94	0.660	1.8504	.3464	.9364
37	0.180	3.3784	.3188	.7184	95	0.680	1.8641	.3335	.9297
38	0.185	3.3700	.3207	.7373	96	0.700	1.8539	.3240	.9262
39	0.190	3.2925	.3349	.7479	97	0.720	1.8087	.3248	.9324
40	0.195	3.1564	.3598	.7583	98	0.740	1.7404	.3340	.9329
41	0.200	3.0752	.3731	.7675	99	0.760	1.6249	.3525	.9301
42	0.205	3.0150	.3819	.7810	100	0.780	1.5004	.3722	.9273
43	0.210	2.9715	.3888	.7953	101	0.800	1.3918	.3878	.9289
44	0.215	2.9635	.3887	.8113	102	0.820	1.3242	.3937	.9369
45	0.220	2.9640	.3847	.8312	103	0.840	1.2439	.4014	.9474
46	0.225	2.9688	.3795	.8427	104	0.860	1.1514	.4123	.9558
47	0.230	2.9723	.3754	.8488	105	0.880	1.0699	.4200	.9691
48	0.235	3.0277	.3608	.8568	106	0.900	1.0085	.4245	.9770
49	0.240	3.0573	.3506	.8661	107	0.920	.9593	.4272	.9816
50	0.245	3.0717	.3424	.8777	108	0.940	.9285	.4270	.9815
51	0.250	3.0281	.3476	.8873	109	0.960	.9127	.4234	.9826
52	0.255	2.9637	.3574	.8959	110	0.980	.8697	.4251	.9817
53	0.260	2.9213	.3626	.9043	111	1.000	.8053	.4308	.9806
54	0.265	2.9259	.3580	.9102	112	1.020	.7627	.4330	.9815
55	0.270	2.9561	.3480	.9141	113	1.040	.7198	.4353	.9857
56	0.275	2.9992	.3359	.9135	114	1.060	.6922	.4345	.9891
57	0.280	3.0841	.3153	.9109	115	1.080	.7137	.4242	.9922
58	0.285	3.1183	.3051	.9095					

Table 1. Regression coefficients and standard deviation (continued)

Mathematical model: $\ln SA(T; \xi = 0.05) = b_1 + b_2 M + \sigma_{\ln SA}^P$

No.	Period $T(s)$	b_1	b_2	$\sigma_{\ln SA}$	No.	Period $T(s)$	b_1	b_2	$\sigma_{\ln SA}$
116	1.100	.7185	.4168	.9936	170	2.18	-1.2319	.5751	1.0616
117	1.120	.6945	.4154	.9950	171	2.20	-1.2606	.5776	1.0660
118	1.140	.6432	.4188	.9977	172	2.22	-1.2887	.5800	1.0705
119	1.160	.5621	.4289	1.0044	173	2.24	-1.3159	.5822	1.0748
120	1.180	.4509	.4457	1.0102	174	2.26	-1.3459	.5851	1.0786
121	1.200	.3473	.4615	1.0132	175	2.28	-1.3889	.5910	1.0813
122	1.220	.2417	.4781	1.0146	176	2.30	-1.4276	.5962	1.0843
123	1.240	.1555	.4908	1.0163	177	2.32	-1.4577	.5997	1.0869
124	1.260	.0765	.5026	1.0172	178	2.34	-1.4842	.6027	1.0885
125	1.280	.0067	.5126	1.0159	179	2.36	-1.5098	.6054	1.0906
126	1.300	-.0708	.5240	1.0119	180	2.38	-1.5399	.6091	1.0926
127	1.320	-.1489	.5354	1.0088	181	2.40	-1.5654	.6119	1.0948
128	1.340	-.2185	.5444	1.0063	182	2.42	-1.5891	.6142	1.0969
129	1.360	-.2647	.5483	1.0036	183	2.44	-1.6144	.6169	1.0988
130	1.380	-.2964	.5489	1.0029	184	2.46	-1.6383	.6192	1.1007
131	1.400	-.3206	.5483	1.0027	185	2.48	-1.6509	.6190	1.1029
132	1.420	-.3414	.5469	1.0014	186	2.50	-1.6598	.6181	1.1053
133	1.440	-.3578	.5454	1.0007	187	2.52	-1.6682	.6170	1.1077
134	1.460	-.3698	.5437	.9982	188	2.54	-1.6760	.6158	1.1102
135	1.480	-.3742	.5400	.9975	189	2.56	-1.6840	.6149	1.1130
136	1.500	-.3852	.5377	.9978	190	2.58	-1.6921	.6139	1.1158
137	1.520	-.3935	.5348	1.0003	191	2.60	-1.6999	.6128	1.1181
138	1.540	-.4067	.5334	1.0022	192	2.62	-1.7102	.6123	1.1198
139	1.560	-.4196	.5323	1.0037	193	2.64	-1.7167	.6111	1.1218
140	1.580	-.4366	.5317	1.0061	194	2.66	-1.7214	.6094	1.1240
141	1.600	-.4587	.5319	1.0091	195	2.68	-1.7237	.6072	1.1265
142	1.620	-.4823	.5324	1.0126	196	2.70	-1.7256	.6051	1.1293
143	1.640	-.5046	.5326	1.0171	197	2.72	-1.7267	.6027	1.1313
144	1.660	-.5295	.5338	1.0212	198	2.74	-1.7341	.6017	1.1340
145	1.680	-.5525	.5344	1.0242	199	2.76	-1.7380	.5999	1.1366
146	1.700	-.5683	.5338	1.0248	200	2.78	-1.7359	.5970	1.1395
147	1.720	-.5975	.5360	1.0254	201	2.80	-1.7288	.5930	1.1425
148	1.740	-.6287	.5383	1.0267	202	2.82	-1.7194	.5886	1.1444
149	1.760	-.6594	.5403	1.0282	203	2.84	-1.7062	.5837	1.1466
150	1.780	-.6846	.5412	1.0297	204	2.86	-1.6903	.5782	1.1482
151	1.800	-.7036	.5408	1.0313	205	2.88	-1.6726	.5723	1.1495
152	1.820	-.7215	.5405	1.0317	206	2.90	-1.6593	.5674	1.1507
153	1.840	-.7630	.5452	1.0305	207	2.92	-1.6449	.5625	1.1523
154	1.860	-.8017	.5489	1.0305	208	2.94	-1.6423	.5600	1.1531
155	1.880	-.8405	.5527	1.0301	209	2.96	-1.6424	.5580	1.1533
156	1.900	-.8718	.5550	1.0290	210	2.98	-1.6424	.5559	1.1533
157	1.920	-.8930	.5554	1.0272	211	3.00	-1.6453	.5546	1.1537
158	1.940	-.9144	.5561	1.0271	212	3.20	-1.6850	.5418	1.1463
159	1.960	-.9402	.5579	1.0271	213	3.40	-1.6284	.5058	1.1332
160	1.980	-.9728	.5609	1.0275	214	3.60	-1.5659	.4731	1.1201
161	2.000	-.9969	.5621	1.0287	215	3.80	-1.4483	.4317	1.1219
162	2.020	-1.0195	.5628	1.0301	216	4.00	-1.4885	.4250	1.1260
163	2.040	-1.0407	.5631	1.0326	217	4.20	-1.4741	.4068	1.1189
164	2.060	-1.0608	.5630	1.0357	218	4.40	-1.5439	.4077	1.1092
165	2.080	-1.0843	.5637	1.0395	219	4.60	-1.5134	.3894	1.1086
166	2.100	-1.1171	.5663	1.0435	220	4.80	-1.4543	.3646	1.1133
167	2.120	-1.1532	.5699	1.0476	221	5.00	-1.3966	.3383	1.1119
168	2.140	-1.1833	.5723	1.0519					
169	2.160	-1.2098	.5741	1.0565					

Table 2. Regression coefficients and standard deviation
Mathematical model: $\ln SA(T; \xi = 0.05) = b_1 + b_2 M + b_3 \ln R_h + \sigma_{\ln SA}^P$

No	Period T (s)	b_1	b_2	b_3	$\sigma_{\ln SA}$
1	0.0100	3.7204	.4090	-.5851	.5708
2	0.0145	3.6740	.4073	-.5560	.5621
3	0.0190	3.7231	.4421	-.6348	.5612
4	0.0235	3.5984	.4625	-.6123	.5614
5	0.0280	3.5934	.4198	-.5241	.5510
6	0.0325	3.7016	.4436	-.5969	.5491
7	0.0370	3.7999	.4056	-.5549	.5564
8	0.0415	3.9480	.4084	-.5950	.5631
9	0.0460	4.0799	.4173	-.6462	.5467
10	0.0505	4.1313	.4008	-.6263	.5449
11	0.0550	4.1950	.4047	-.6316	.5477
12	0.0595	4.1988	.3835	-.5708	.5378
13	0.0640	4.1840	.3655	-.5154	.5547
14	0.0685	4.1325	.3276	-.4119	.5624
15	0.0730	4.0372	.3123	-.3279	.5787
16	0.0775	4.1435	.2953	-.3173	.5583
17	0.0820	4.1716	.3147	-.3478	.5439
18	0.0865	4.2335	.2960	-.3259	.5353
19	0.0910	4.2510	.2578	-.2512	.5241
20	0.0955	4.4854	.2171	-.2456	.5426
21	0.10	4.7439	.2210	-.3302	.5534
22	0.105	4.8393	.2435	-.3962	.5705
23	0.11	5.0188	.2415	-.4628	.5911
24	0.115	5.0740	.2540	-.5044	.6209
25	0.12	5.2457	.2788	-.6092	.6284
26	0.125	5.2854	.2772	-.6139	.6210
27	0.13	5.2426	.3027	-.6353	.6221
28	0.135	5.0579	.3344	-.6212	.6539
29	0.14	4.8822	.3792	-.6394	.6721
30	0.145	4.7554	.4069	-.6489	.6837
31	0.15	4.5899	.4295	-.6346	.6814
32	0.155	4.4436	.4351	-.5978	.6758
33	0.16	4.4014	.4371	-.5905	.6702
34	0.165	4.4134	.4308	-.5838	.6659
35	0.17	4.4161	.4307	-.5829	.6667
36	0.175	4.3809	.4442	-.5939	.6789
37	0.18	4.3734	.4417	-.5867	.6997
38	0.185	4.4082	.4489	-.6121	.7173
39	0.19	4.3462	.4650	-.6212	.7275
40	0.195	4.1859	.4869	-.6070	.7396
41	0.20	4.0802	.4972	-.5926	.7505
42	0.205	3.9833	.5014	-.5709	.7662
43	0.21	3.9132	.5050	-.5552	.7822
44	0.215	3.9139	.5060	-.5604	.7983
45	0.22	3.9324	.5043	-.5710	.8182
46	0.225	3.9789	.5042	-.5956	.8283
47	0.23	4.0118	.5038	-.6129	.8333
48	0.235	4.0855	.4914	-.6237	.8407
49	0.24	4.0720	.4759	-.5983	.8523
50	0.245	4.0418	.4622	-.5720	.8661
51	0.25	3.9997	.4676	-.5730	.8760
52	0.255	3.9366	.4775	-.5736	.8848
53	0.26	3.8973	.4830	-.5754	.8933
54	0.265	3.9178	.4804	-.5848	.8988
55	0.27	3.9558	.4714	-.5894	.9025
56	0.275	3.9786	.4568	-.5774	.9027
57	0.28	4.0643	.4363	-.5779	.9000
58	0.285	4.0948	.4257	-.5757	.8987

No	Period T (s)	b_1	b_2	b_3	$\sigma_{\ln SA}$
59	0.29	4.1080	.4170	-.5724	.9029
60	0.295	4.1121	.4061	-.5618	.9082
61	0.30	4.1000	.3945	-.5431	.9196
62	0.305	4.0876	.3864	-.5298	.9295
63	0.31	4.1066	.3900	-.5474	.9352
64	0.315	4.0853	.3943	-.5497	.9370
65	0.32	4.0721	.3979	-.5557	.9409
66	0.325	4.0628	.4007	-.5624	.9454
67	0.33	4.0502	.4102	-.5799	.9482
68	0.335	4.0445	.4192	-.6007	.9502
69	0.34	4.0270	.4296	-.6189	.9465
70	0.345	3.9883	.4401	-.6293	.9385
71	0.35	3.9691	.4462	-.6400	.9296
72	0.355	3.9764	.4489	-.6547	.9205
73	0.36	4.0185	.4484	-.6762	.9127
74	0.365	4.0733	.4485	-.7037	.9064
75	0.37	4.1194	.4575	-.7420	.9062
76	0.375	4.1403	.4675	-.7733	.9045
77	0.38	4.1515	.4763	-.7992	.9044
78	0.385	4.1564	.4832	-.8188	.9039
79	0.39	4.1646	.4867	-.8331	.9006
80	0.395	4.1641	.4890	-.8407	.8959
81	0.40	4.1729	.4903	-.8491	.8941
82	0.42	4.1658	.4945	-.8691	.9046
83	0.44	4.2230	.4712	-.8681	.9089
84	0.46	4.0701	.4671	-.8306	.9167
85	0.48	3.9697	.4686	-.8251	.9207
86	0.50	3.8556	.4951	-.8491	.9118
87	0.52	3.7150	.5180	-.8556	.9040
88	0.54	3.5437	.5419	-.8566	.8944
89	0.56	3.4334	.5657	-.8831	.8957
90	0.58	3.4177	.5735	-.9120	.8968
91	0.60	3.4229	.5697	-.9291	.9043
92	0.62	3.4875	.5642	-.9618	.9091
93	0.64	3.4904	.5576	-.9657	.9022
94	0.66	3.4955	.5495	-.9699	.8916
95	0.68	3.5027	.5358	-.9661	.8849
96	0.70	3.5081	.5282	-.9753	.8801
97	0.72	3.4841	.5316	-.9878	.8853
98	0.74	3.4192	.5412	-.9898	.8856
99	0.76	3.3057	.5600	-.9910	.8824
100	0.78	3.1797	.5795	-.9901	.8796
101	0.80	3.0627	.5941	-.9852	.8818
102	0.82	2.9928	.5997	-.9838	.8906
103	0.84	2.9076	.6067	-.9810	.9021
104	0.86	2.7893	.6145	-.9657	.9128
105	0.88	2.6843	.6192	-.9518	.9285
106	0.90	2.5900	.6197	-.9324	.9389
107	0.92	2.5120	.6189	-.9155	.9454
108	0.94	2.4430	.6140	-.8930	.9476
109	0.96	2.3961	.6065	-.8746	.9505
110	0.98	2.3424	.6070	-.8683	.9501
111	1.00	2.2930	.6145	-.8772	.9481
112	1.02	2.2642	.6183	-.8852	.9483
113	1.04	2.2348	.6224	-.8932	.9520
114	1.06	2.2306	.6245	-.9071	.9542
115	1.08	2.2809	.6176	-.9240	.9558

Table 2. Regression coefficients and standard deviation (continued)
Mathematical model: $\ln SA(T; \xi = 0.05) = b_1 + b_2 M + b_3 \ln R_h + \sigma_{\ln SA}^P$

No	Period T (s)	b_1	b_2	b_3	$\sigma_{\ln SA}$	No	Period T (s)	b_1	b_2	b_3	$\sigma_{\ln SA}$
116	1.10	2.3080	.6130	-.9372	.9559	170	2.18	.2453	.7574	-.8710	1.0337
117	1.12	2.2819	.6114	-.9359	.9576	171	2.20	.2215	.7605	-.8738	1.0381
118	1.14	2.2241	.6140	-.9321	.9608	172	2.22	.2003	.7639	-.8779	1.0424
119	1.16	2.1449	.6243	-.9332	.9677	173	2.24	.1810	.7670	-.8825	1.0465
120	1.18	2.0273	.6403	-.9295	.9743	174	2.26	.1527	.7701	-.8836	1.0504
121	1.20	1.9223	.6560	-.9286	.9775	175	2.28	.0926	.7739	-.8735	1.0541
122	1.22	1.8041	.6710	-.9212	.9797	176	2.30	.0425	.7777	-.8668	1.0577
123	1.24	1.7032	.6819	-.9125	.9824	177	2.32	.0046	.7803	-.8622	1.0609
124	1.26	1.6077	.6916	-.9028	.9843	178	2.34	-.0277	.7825	-.8587	1.0628
125	1.28	1.5136	.6986	-.8885	.9842	179	2.36	-.0578	.7847	-.8561	1.0652
126	1.30	1.4219	.7083	-.8801	.9808	180	2.38	-.1021	.7866	-.8477	1.0681
127	1.32	1.3340	.7184	-.8743	.9781	181	2.40	-.1466	.7871	-.8365	1.0712
128	1.34	1.2590	.7268	-.8711	.9758	182	2.42	-.1872	.7873	-.8266	1.0742
129	1.36	1.2206	.7317	-.8757	.9725	183	2.44	-.2291	.7879	-.8168	1.0770
130	1.38	1.2051	.7343	-.8852	.9708	184	2.46	-.2686	.7883	-.8076	1.0797
131	1.40	1.1966	.7356	-.8946	.9697	185	2.48	-.2933	.7866	-.8004	1.0825
132	1.42	1.1959	.7367	-.9064	.9673	186	2.50	-.3146	.7842	-.7932	1.0855
133	1.44	1.1933	.7369	-.9145	.9657	187	2.52	-.3346	.7817	-.7863	1.0885
134	1.46	1.1741	.7343	-.9103	.9635	188	2.54	-.3532	.7791	-.7799	1.0915
135	1.48	1.1659	.7302	-.9080	.9630	189	2.56	-.3723	.7768	-.7734	1.0950
136	1.50	1.1490	.7271	-.9046	.9636	190	2.58	-.3887	.7748	-.7685	1.0982
137	1.52	1.1462	.7249	-.9078	.9660	191	2.60	-.4058	.7725	-.7630	1.1009
138	1.54	1.1424	.7246	-.9133	.9675	192	2.62	-.4261	.7708	-.7571	1.1032
139	1.56	1.1374	.7245	-.9180	.9686	193	2.64	-.4349	.7693	-.7557	1.1053
140	1.58	1.1304	.7252	-.9239	.9705	194	2.66	-.4374	.7680	-.7570	1.1075
141	1.60	1.1178	.7265	-.9295	.9731	195	2.68	-.4353	.7663	-.7596	1.1099
142	1.62	1.1110	.7291	-.9394	.9758	196	2.70	-.4322	.7648	-.7626	1.1126
143	1.64	1.1098	.7320	-.9519	.9793	197	2.72	-.4291	.7629	-.7650	1.1145
144	1.66	1.1065	.7357	-.9646	.9823	198	2.74	-.4403	.7614	-.7628	1.1174
145	1.68	1.1035	.7389	-.9764	.9843	199	2.76	-.4432	.7598	-.7634	1.1201
146	1.70	1.0976	.7395	-.9822	.9844	200	2.78	-.4350	.7576	-.7670	1.1228
147	1.72	1.0592	.7405	-.9768	.9856	201	2.80	-.4182	.7548	-.7728	1.1255
148	1.74	1.0171	.7415	-.9703	.9877	202	2.82	-.3993	.7516	-.7783	1.1271
149	1.76	.9811	.7428	-.9672	.9895	203	2.84	-.3711	.7486	-.7872	1.1287
150	1.78	.9537	.7434	-.9659	.9912	204	2.86	-.3426	.7446	-.7946	1.1298
151	1.80	.9339	.7429	-.9655	.9930	205	2.88	-.3148	.7400	-.8006	1.1307
152	1.82	.9040	.7412	-.9584	.9941	206	2.90	-.2917	.7362	-.8064	1.1315
153	1.84	.8288	.7417	-.9385	.9948	207	2.92	-.2599	.7335	-.8166	1.1324
154	1.86	.7631	.7421	-.9226	.9961	208	2.94	-.2528	.7315	-.8193	1.1331
155	1.88	.6965	.7424	-.9062	.9975	209	2.96	-.2509	.7298	-.8204	1.1332
156	1.90	.6310	.7405	-.8860	.9982	210	2.98	-.2503	.7277	-.8208	1.1331
157	1.92	.5729	.7364	-.8643	.9983	211	3.00	-.2567	.7260	-.8187	1.1337
158	1.94	.5284	.7343	-.8507	.9993	212	3.20	-.3686	.7043	-.7761	1.1292
159	1.96	.4790	.7331	-.8368	1.0006	213	3.40	-.2705	.6734	-.8006	1.1138
160	1.98	.4279	.7338	-.8258	1.0020	214	3.60	-.2057	.6410	-.8020	1.1002
161	2.00	.3951	.7339	-.8207	1.0037	215	3.80	-.0447	.6049	-.8275	1.1001
162	2.02	.3772	.7353	-.8235	1.0049	216	4.00	-.1111	.5950	-.8121	1.1055
163	2.04	.3699	.7373	-.8317	1.0068	217	4.20	-.0850	.5783	-.8190	1.0977
164	2.06	.3677	.7394	-.8423	1.0092	218	4.40	-.2000	.5736	-.7923	1.0896
165	2.08	.3620	.7422	-.8527	1.0122	219	4.60	-.1900	.5528	-.7802	1.0899
166	2.10	.3404	.7463	-.8594	1.0158	220	4.80	-.1139	.5301	-.7903	1.0940
167	2.12	.3072	.7501	-.8610	1.0199	221	5.00	-.0591	.5034	-.7886	1.0927
168	2.14	.2787	.7527	-.8620	1.0244						
169	2.16	.2585	.7553	-.8657	1.0288						

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